

# Appendix to the Computer Manual in MATLAB to accompany Pattern Classification (2nd ed.)

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## Preface

This Appendix is a pre-publication version to be included in the furthcoming version of the **Computer Manual to accompany Pattern Classification**, 2<sup>nd</sup> Edition. It includes short descriptions of the programs in the classification toolbox invoked directly by users.

Additional information and updates are available from the authors' web site at http://www.yom-tov.info

We wish you the best of luck in your studies and research!

David G. Stork Elad Yom-Tov

#### APPENDIX

## Program descriptions

Below are short descriptions of the programs in the classification toolbox invoked directly by users. This listings are organized by chapter in **Pattern Classification**, and in some cases include pseudo-code. Not all programs here appear in the textbook and not every minor variant on an algorithm in the textbook appears here. While most classification programs take input data sets and targets, some classification and feature selection programs have associated additional inputs and outputs, as listed. You can obtain further specific information on the algorithms by consulting **Pattern Classification** and information on the MATLAB code by using its help command.

### Chapter 2

### Marginalization

Function name: Marginalization

#### **Description**:

Compute the marginal distribution of a multi-dimensional histogram or distribution as well as the marginal probabilities for test patterns given the "good" features.

#### Syntax:

predicted\_targets = marginalization(training\_patterns, training\_targets, test\_patterns, parameter vector);

#### **Parameters**:

- 1. The index of the missing feature.
- 2. The number of patterns with which to compute the marginal.

### Minimum cost classifier

Function name: minimum cost

#### **Description**:

Perform minimum-cost classification for known distributions and cost matrix  $\lambda_{ij}$ .

#### Syntax:

predicted\_targets = minimum\_cost(training\_patterns, training\_targets, test\_patterns, parameter vector);

#### Parameter:

The cost matrix  $\lambda_{ij}$ .

### **Normal Density Discriminant Function**

#### Function name: NNDF

#### **Description**:

Construct the Bayes classifier by computing the mean and d-by-d covariance matrix of each class and then use them to construct the Bayes decision region.

#### Syntax:

predicted\_targets = NNDF(training\_patterns, training\_targets, test\_patterns, parameter vector);

#### **Parameters**:

The discriminant function (probability) for any test pattern.

### **Stumps**

Function name: Stumps

#### **Description**:

Determine the threshold value on a single feature that will yield the lowest training error. This classifier can be thought of as a linear classifier with a single weight that differs from zero.

#### Syntax:

predicted\_targets = Stumps(training\_patterns, training\_targets, test\_patterns, parameter vector);

[predicted\_targets, weights] = Stumps(training\_patterns, training\_targets, test\_patterns, parameter vector);

#### **Parameter**:

Optional: A weight vector for the training patterns.

#### Additional outputs:

The weight vector for the linear classifier arising from the optimal threshold value.

### **Discrete Bayes Classifier**

Function name: Discrete\_Bayes

#### **Description**:

Perform Bayesian classification on feature vectors having discrete values. In this implementation, discrete features are those that have no more than one decimal place. The program bins the data and then computes the probability of each class. The program then computes the classification decision based on standard Bayes theory.

#### Syntax:

predicted\_targets = Discrete\_Bayes(training\_patterns, training\_targets, test\_patterns, parameter vector);

#### Parameters:

None

### **Multiple Discriminant Analysis**

Function name: MultipleDiscriminantAnalysis

#### **Description**:

Find the discriminants for a multi-category problem. The discriminant maximizes the ratio of the between-class variance to that of the in-class variance.

#### Syntax:

[new\_patterns, new\_targets] = MultipleDiscriminantAnalysis(training\_patterns, training\_targets);

[new\_patterns, new\_targets, feature\_weights] = MultipleDiscriminantAnalysis(training\_patterns, training\_targets);

#### Additional outputs:

The weight vectors for the discriminant boundaries.

### Bhattacharyya

Function name: Bhattacharyya

#### **Description**:

Estimate the Bhattacharyya error rate for a two-category problem, assuing Gaussianity. The bound is given by:

$$k\left(\frac{1}{2}\right) = \frac{1}{8}(\mu_1 - \mu_2)^t (\Sigma_1 - \Sigma_2)^{-1}(\mu_1 - \mu_2) + \frac{1}{2}\ln\frac{|\Sigma_1 - \Sigma_2|}{2\sqrt{|\Sigma_1||\Sigma_2|}}$$

#### Syntax:

error\_bound = Bhattacharyya(mu1, sigma1, mu2, sigma2, p1);

#### Input variables:

- 1. mu1, mu2 The means of class 1 and 2, respectively.
- 2. sigma1, sigma2 The covariance of class 1 and 2, respectively.
- 3. p1 The probability of class 1.

### Chernoff

Function name: Chernoff

#### **Description**:

Estimate the Chernoff error rate for a two-category problem. The error rate is computed through the following equation:

$$min_{\beta} \left\{ e^{-\left[\beta \frac{(1-\beta)}{2}(\mu_{2}-\mu_{1})^{T} \left[\beta \Sigma_{1}+(1-\beta)\Sigma_{2}\right]^{-1}(\mu_{2}-\mu_{1})+\frac{1}{2} ln \left|\frac{\beta \Sigma_{1}+(1-\beta)\Sigma_{2}}{|\Sigma_{1}|^{\beta} |\Sigma_{2}|^{1-\beta}}\right]\right\} \right\}$$

#### Syntax:

error\_bound = Chernoff(mu1, sigma1, mu2, sigma2, p1);

#### Input variables:

- 1. mu1, mu2 The means of class 1 and 2, respectively.
- 2. sigma1, sigma2 The covariance of class 1 and 2, respectively.
- 3. p1 The probability of class 1.

### Discriminability

Funciton name: Discriminability

**Description**: Compute the discriminability d' in the Receiver Operating Characteristic (ROC) curve.

### Syntax:

d\_tag = Discriminability(mu1, sigma1, mu2, sigma2, p1);

#### Input variables:

- 1. mu1, mu2 The means of class 1 and 2, respectively.
- 2. sigma1, sigma2 The covariance of class 1 and 2, respectively.
- 3. p1 The probability of class 1.

### Chapter 3

### Maximum-Likelihood Classifier

Function name: ML

#### **Description**:

Compute the maximum-likelihood estimate of the mean and covariance matrix of each class and then uses the results to construct the Bayes decision region. This classifier works well if the classes are uni-modal, even when they are not linearly seperable.

#### Syntax:

predicted\_targets = ML(training\_patterns, training\_targets, test\_patterns, []);

## Maximum-Likelihood Classifier assuming Diagonal Covariance Matrices

Function name: ML\_diag

#### **Description**:

Compute the maximum-likelihood estimate of the mean and covariance matrix (assumed diagonal) of each class and then uses the results to construct the Bayes decision region. This classifier works well if the classes are unimodal, even when they are not linearly separable.

#### Syntax:

predicted\_targets = ML\_diag(training\_patterns, training\_targets, test\_patterns, []);

### Gibbs

Function name: Gibbs

#### **Description**:

This program finds the probability that the training data comes from a Gaussian distribution with known parameters, i.e.,  $P(D|\theta)$ . Then, using  $P(D|\theta)$ , the program samples the parameters according to the Gibbs method, and finally uses the parameters to classify the test patterns.

#### Syntax:

predicted\_targets = Discrete\_Bayes(training\_patterns, training\_targets, test\_patterns, input parameter);

#### Parameter:

Resolution of the input features (i.e., the number of bins).

### **Fishers Linear Discriminant**

Function name: FishersLinearDiscriminant

#### Description:

Computes the Fisher linear discriminant for a pair of distributions. The Fisher linear discriminant attempts to maximize the ratio of the between-class variance to that of the in-class variance. This is done by reshaping the data through a linear weight vector computed by the equasion:

 $w \, = \, S_W^{-1}(m_1^{} - m_2^{})$ 

where  $S_W$  is the in-class (or within-class) scatter matrix.

#### Syntax:

[new\_patterns, new\_targets] = FishersLinearDiscriminant(training\_patterns, training\_targets, [], []);

[new\_patterns, new\_targets, weights] = FishersLinearDiscriminant(training\_patterns, training\_targets, [], []);

#### Additional outputs:

The weight vector for the linear classifier.

### Local Polynomial Classifier

Function name: Local\_Polynomial

**Description**: This nonlinear classification algorithm works by building a classifier based on a local subset of training points, and classifies the test points according to those local classifiers. The method randomly selects a predetermined number of the training points and then assign each of the test points to the nearest of the points so selected. Next, the method builds a logistic classifier around these selected points, and finally classifies the points assigned to it.

#### Syntax:

predicted\_targets = Local\_Polynomial(training\_patterns, training\_targets, test\_patterns, input parameter);

#### Input parameter:

Number of (local) points to select for creation of a local polynomial or logistic classifier.

### **Expectation-Maximization**

Function name: Expectation\_Maximization

#### **Description**:

Estimate the means and covariances of component Gaussians by the method of expectation-maximization.

#### Pseudo-code:

```
<u>begin initialize</u> θ<sub>0</sub>, T, i ← 0

<u>do</u> i ← i + 1

E step: compute Q(\theta; \theta^i)

M step: \theta^{i+1} \leftarrow argmax_{\theta}Q(\theta; \theta^i)

<u>until</u> Q(\theta^{i+1}; \theta^i) - Q(\theta^i; \theta^{i-1}) \le T

<u>return</u> \hat{\theta} \leftarrow \theta^{i+1}
```

#### end

#### Syntax:

predicted\_targets = EM(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, estimated\_parameters] = EM(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Program descriptions

#### Input parameters:

The number of Gaussians for each class.

#### Additional outputs:

The estimated means and covariances of Gaussians.

#### Example:



These figures show the results of running the EM algorithm with different parameter values. The left figure shows the decision region obtained when the wrong number of Gaussians is entered, while the right shows the decision region when the correct number of Gaussians in each class is entered.

### **Multivariate Spline Classification**

Function name: Multivariate\_Splines

#### **Description**:

This algorithm fits a spline to the histogram of each of the features of the data. The algorithm then selects the spline that reduces the training error the most, and computes the associated residual of the prediction error. The process iterates on the remaining features, until all have been used. Then, the prediction of each spline is evaluated independently, and the weight of each spline is computed via the pseudo-inverse. This algorithm is typically used for regression but here is used for classification.

#### Syntax:

predicted\_targets = Multivariate\_Splines(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

- 1. The degree of the splines.
- 2. The number of knots per spline.

### Whitening transform

Function name: Whitening\_transform

#### **Description**:

Apply the whitening transform to a d-dimensional data set. The algorithm first subtracts the sample mean from each point, and then multiplies the data set by the inverse of the square root of the covariance matrix.

#### Syntax:

[new\_patterns, new\_targets] = Whitening\_transform(training\_patterns, training\_targets, [], []);

[new\_patterns, new\_targets, means, whiten\_mat] = Whitening\_transform(training\_patterns, training\_targets, [], []);

#### Additional outputs:

- 1. The whitening matrix.
- 2. The means vector.

### **Scaling transform**

Function name: Scaling\_transform

#### **Description**:

Standardize the data, that is, transforms a data set so that it has zero mean and unit variance along each coordinate. This scaling is recommended as preprocessing for data presented to a neural network classifier.

#### Syntax:

[new\_patterns, new\_targets] = Scaling\_transform(training\_patterns, training\_targets, [], []);

[new\_patterns, new\_targets, means, variance\_mat] = Scaling\_transform(training\_patterns, training\_targets, [], []);

#### Additional outputs:

1. The variance matrix.

2. The means vector.

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### Hidden Markov Model Forward Algorithm

Function name: HMM\_Forward

#### **Description**:

Compute the probability that a test sequence  $V^T$  was generated by a given hidden Markov model according to the Forward algorithm. Note: This algorithm is in the "Other" subdirectory.

#### Pseudo-code:

**<u>begin initialize</u>**  $t \leftarrow 0$ ,  $a_{ij}$ ,  $b_{jk}$ , visible sequence  $\mathbf{V}^{\mathrm{T}}$ ,  $\alpha_{i}(0)$ 

for 
$$t \leftarrow t+1$$
  
 $\beta_i(t) \leftarrow \sum_{j=1}^c \beta_j(t+1)a_{ij}b_{jk}v(t+1)$ 

until t=T

**<u>return</u>**  $P(V^T) \leftarrow \alpha_0(T)$  for the final state

<u>end</u>

Syntax:

[Probability\_matrix, Probability\_matrix\_through\_estimation\_stages] = HMM\_Forward(Transition\_prob\_matrix, Output\_generation\_mat, Initial\_state, Observed output sequence);

### Hidden Markov Model Backward Algorithm

Function name: HMM Backward

#### **Description**:

Compute the probability that a test sequence  $V^T$  was generated by a given hidden Markov model according to the Backward algorithm. Learning in hidden Markov models via the Forward-Backward algorithm makes use of both the Forward and the Backward algorithms. Note: This algorithm is in the "Other" subdirectory.

#### Pseudo-code:

**<u>begin initialize</u>**  $\beta_i(T)$ ,  $t \leftarrow T$ ,  $a_{ij}$ ,  $b_{jk}$ , visible sequence  $\mathbf{V}^T$ 

$$\underbrace{\mathbf{for}}_{ji} \quad t \leftarrow t - 1$$
$$\beta_i(t) \leftarrow \sum_{i=1}^c \beta_j(t+1) a_{ij} b_{jk} v(t+1)$$

<u>until</u> t=1

**<u>return</u>**  $P(V^T) \leftarrow \beta_i(0)$  for the known initial state

end

#### Syntax:

[Probability\_matrix, Probability\_matrix\_through\_estimation\_stages] = HMM\_Backward(Transition\_prob\_matrix, Output\_generation\_mat, Final\_state, Observed output sequence);

### **Forward-Backward Algorithm**

Function name: HMM\_Forward\_Backward

#### **Description**:

Estimate the parameters in a hidden Markov model based on a set of training sequences. Note: This algorithm is in the "Other" subdirectory.

#### Pseudo-code:

.

**<u>begin initialize</u>**  $a_{ij}$ ,  $b_{jk}$ , training sequence  $V^T$ , convergence criterion  $\theta$ ,  $z \leftarrow 0$ 

$$\frac{\mathbf{do}}{\mathbf{c}} z \leftarrow z + 1$$
compute  $\hat{a}(z)$  from  $a(z-1)$  and  $b(z-1)$ 
compute  $\hat{b}(z)$  from  $a(z-1)$  and  $b(z-1)$ 
 $a_{ij}(z) \leftarrow \hat{a}_{ij}(z-1)$ 
 $b_{jk}(z) \leftarrow \hat{b}_{jk}(z-1)$ 

$$\mathbf{until} \ max_{i,j,k} \left[ a_{ij}(z) - a_{ij}(z-1), b_{jk}(z) - b_{jk}(z-1) \right] < \theta$$
return  $a_{ij} \leftarrow a_{ij}(z), \ b_{jk} \leftarrow b_{jk}(z)$ 

end

#### Syntax:

[Estimated\_Transition\_Probability\_matrix, Estimated\_Output\_Generation\_matrix] = HMM\_Forward\_backward(Transition\_prob\_matrix, Output\_generation\_mat, Observed output sequence);

### **Hidden Markov Model Decoding**

Function name: HMM\_Decoding

#### **Description**:

Estimate a highly likely path through the hidden Markov model (trellis) based on the topology and transition probabilities in that model. Note: This algorithm is in the "Other" subdirectory.

#### **Pseudo-code:**

```
begin initialize Path \leftarrow \{ ... \}, t \leftarrow 0

for t \leftarrow t + 1

for j \leftarrow j + 1

\alpha_j(t) \leftarrow b_{jk}v(t)\sum_{i=1}^c \alpha_i(t-1)a_{ij}

until j = c

j' \leftarrow \arg max_j\alpha_j(t)

Append \omega_{j'} to Path

until t = T

return Path
```

end

#### Syntax:

Likely\_sequence = HMM\_Forward(Transition\_prob\_matrix, Output\_generation\_mat, Initial\_state, Observed output sequence);

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### Chapter 4

### **Nearest-Neighbor Classifier**

Function name: Nearest\_Neighbor

#### **Description**:

For each of the test examples, the nearest k neighbors from training examples are found, and the majority label among these are given as the label to the test example. The number of nearest neighbors determines how local the classifier is. If this number is small, the classifier is more localized. This classifier usually results in reasonably low training error, but it is expensive computationally and memory-wise.

#### Syntax:

predicted\_targets = Nearest\_Neighbor(training\_patterns, training\_targets, test\_patterns, input parameter);

#### Input parameters:

Number of nearest neighbors, k.

### **Nearest-Neighbor Editing**

Function name: NearestNeighborEditing

#### **Description**:

This algorithm searches for the Voronoi neighbors of each pattern. If the labels of all the neighbors are the same, the pattern in discarded. The MATLAB implementation uses linear programming to increase speed. This algorithm can be used for reducing the number of training data points.

#### Pseudo-code:

**begin initialize**  $j \leftarrow 0$ ,  $D \leftarrow data set, n \leftarrow num prototypes$ construct the full Voronoid diagram of D **<u>do</u>**  $j \leftarrow j + 1$ ; for each prototype  $x_j'$ find the Voronoi neighbors of  $x_i$ **<u>if</u>** any neighbor is not from the same class as  $x_i'$  **<u>then</u>** mark  $x_i'$ **<u>until</u>** j = ndiscard all points that are not marked construct the Voronoi diagram of the remaining (marked) prototypes end

#### Syntax:

[new\_patterns, new\_targets] = NearestNeighborEditing(training\_patterns, training\_targets, [], []);

### **Store-Grabbag Algorithm**

Function name: Store\_Grabbag

#### **Description**:

The store-grabbag algorithm is a modification of the nearest-neighbor algorithm. The algorithm identifies those samples in the training set that affect the classification, and discards the others.

#### Syntax:

predicted\_targets = Store\_Grabbag(training\_patterns, training\_targets, test\_patterns, input parameter);

#### Input parameter:

Number of nearest neighbors, k.

### **Reduced Coloumb Energy**

Function name: RCE

**Description**: Create a classifier based on a training set, maximizing the radius around each training point (up to  $\lambda_{max}$ ) yet not misclassifying other training points.

#### Pseudo-code:

Training

**<u>begin initialize</u>**  $j \leftarrow 0$ ,  $n \leftarrow num$  patterns,  $\varepsilon \leftarrow small param$ ,  $\lambda_m \leftarrow max$  radius

 $\begin{array}{l} \underline{\mathbf{do}} \quad j \leftarrow j+1 \\ & w_{ij} \leftarrow x_i \text{ (train weight)} \\ & \hat{\mathbf{x}} \leftarrow \arg min_{\mathbf{x} \notin \omega_i} D(\mathbf{x}, \mathbf{x}') \text{ (find nearest point not in } \omega_i) \\ & \lambda_j \leftarrow \min \left[ D(\hat{\mathbf{x}}, \mathbf{x}') - \varepsilon, \lambda_m \right] \quad (\text{set radius}) \\ & \underline{\mathbf{if}} \; x \in \omega_k \; \underline{\mathbf{then}} \; a_{jk} \leftarrow 1 \\ & \underline{\mathbf{until}} \; j = n \end{array}$ 

end
## Classification

$$\begin{array}{l} \underline{\textbf{begin initialize}} \ j \leftarrow 0, \ k \leftarrow 0, \ \textbf{x} \leftarrow test \ pattern, \ \mathbf{D}_t \leftarrow \{...\} \\ \hline \underline{\textbf{do}} \ j \leftarrow j+1 \\ \underline{\textbf{if}} \ D(\textbf{x}, \textbf{x}_j') < \lambda_j \ \underline{\textbf{then}} \ \mathbf{D}_t \leftarrow \mathbf{D}_t \cup \textbf{x}'_j \\ \hline \underline{\textbf{until}} \ j = n \\ \underline{\textbf{if}} \ label of all \ \textbf{x}'_j \in \mathbf{D}_t \ is the same \ \underline{\textbf{then return}} \ label of all \ \textbf{x}_k \in \mathbf{D}_t \\ \underline{\textbf{else return}} \ \text{``ambiguous''} \ label \end{array}$$

<u>end</u>

## Syntax:

predicted\_targets = RCE(training\_patterns, training\_targets, test\_patterns, input parameter);

## Input parameters:

The maximum allowable radius,  $\lambda_{\text{max}}.$ 

# Parzen Windows Classifier

Function name: Parzen

## **Description**:

Estimate a posterior density by convolving the data set in each category with a Gaussian Parzen window of scale h. The scale of the window determines the locality of the classifier such that a larger h causes the classifier to be more global.

## Syntax:

predicted\_targets = Parzen(training\_patterns, training\_targets, test\_patterns, input parameter);

### Input parameter:

Normalizing factor for the window width, h.

# **Probabilistic Neural Network Classification**

### Function name: PNN

## **Description**:

This algorithm trains a probabalistic neural network and uses it to classify test data. The PNN is a parallel implementation of the Parzen windows classifier.

### Pseudo-code

<u>begin initialize</u>  $k \leftarrow 0$ ,  $x \leftarrow test pattern$ 

$$\frac{\mathbf{do}}{\mathbf{b}} k \leftarrow k + 1$$

$$net_k \leftarrow \mathbf{w}_k^t \mathbf{x}$$

$$\mathbf{if} \ a_{ki} = 1 \ \mathbf{then} \ g_i \leftarrow g_i + \exp[(net_k - 1)/\sigma^2]$$

<u>**return**</u> class  $\leftarrow argmax_i g_i(\mathbf{x})$ 

#### end

#### Syntax:

predicted\_targets = PNN(training\_patterns, training\_targets, test\_patterns, input parameter);

## Input parameter:

The Gaussian width,  $\boldsymbol{\sigma}$  .

# Chapter 5

## **Basic Gradient Descent**

Function name: BasicGradientDescent

## **Description**:

Perform simple gradient descent in a scalar-valued criterion function J(a).

#### Pseudo-code:

**<u>begin initialize</u>** *a*, threshold  $\theta$ ,  $\eta$ (.),  $k \leftarrow 0$ 

 $\underline{\mathbf{do}} \ k \leftarrow k + 1$  $\mathbf{a} \leftarrow \mathbf{a} - \eta(k) \nabla J(\mathbf{a})$  $\underline{\mathbf{until}} \ \left| \eta(k) \nabla J(\mathbf{a}) \right| < \theta$ 

#### <u>return</u> a

end

## Syntax:

min\_point = gradient\_descent(Initial search point, theta, eta, function to minimize)

Note: The function to minimize must accept a value and return the function's value at that point.

# **Newton Gradient Descent**

Function name: Newton descent

### **Description**:

Perform Newton's method for gradient descent in a scalar-valued criterion function J(a), where the Hessian matrix H can be computed.

Pseudo-code:

**begin initialize** a, threshold  $\theta$ 

<u>do</u>

 $a \leftarrow a - H^{-1} \nabla J(a)$ 

**<u>until</u>**  $|\boldsymbol{H}^{-1}\nabla J(\boldsymbol{a})| < \theta$ 

<u>return</u> a

<u>end</u>

Syntax:

min\_point = Newton\_descent(Initial search point, theta, function to minimize)

Note: The function to minimize must accept a value and return the function's value at that point.

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## **Batch Perceptron**

Function name: Perceptron\_Batch

#### **Description**:

Train a linear Perceptron classifier in batch mode.

#### Pseudo-code:

**<u>begin initialize</u>** *a*, criterion  $\theta$ ,  $\eta$ (.),  $k \leftarrow 0$ 

$$\underline{\mathbf{do}} \ k \leftarrow k + 1$$

$$a \leftarrow a + \eta(k) \sum_{y \in Y_k} \mathbf{y}$$

$$\underline{\mathbf{until}} \left| \eta(k) \sum_{y \in Y} \mathbf{y} \right| < \theta$$
return a

<u>end</u>

#### Syntax:

predicted\_targets = Perceptron\_Batch(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights] = Perceptron\_Batch(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights, weights\_through\_the\_training] = Perceptron\_Batch(training\_patterns, training\_targets, test\_patterns, input parameters);

## Input parameters:

- 1. The maximum number of iterations.
- 2. The convergence criterion.
- 3. The convergence rate.

## Additional outputs:

- 1. The weight vector for the linear classifier.
- 2. The weights throughout learning.

## **Fixed-Increment Single-Sample Perceptron**

Function name: Perceptron FIS

#### **Description**:

This algorithm attempts to iteratively find a linear separating hyperplane. If the problem is linear, the algorithm is guaranteed to find a solution. During the iterative learning process the algorithm randomly selects a sample from the training set and tests if that sample is correctly classified. If not, the weight vector of the classifier is updated. The algorithm iterates until all training samples are correctly classified or the maximal number of training iterations is reached.

#### Pseudo-code:

#### **begin initialize** $a, k \leftarrow 0$

 $\underline{\mathbf{do}} \ k \leftarrow (k+1) mod \ n$ 

**<u>if</u>**  $\mathbf{y}^k$  is misclassified by a <u>then</u>  $a \leftarrow a + y^k$ 

until all patterns properly classified

<u>return</u> a

end

#### Syntax:

predicted\_targets = Perceptron\_FIS(training\_patterns, training\_targets, test\_patterns, input parameter);

[predicted\_targets, weights] = Perceptron\_FIS(training\_patterns, training\_targets, test\_patterns, input parameter);

## Input parameters:

The parameters describing either the maximum number of iterations, or a weight vector for the training samples, or both.

## Additional outputs:

The weight vector for the linear classifier.

## Variable-increment Perceptron with Margin

Function name: Perceptron\_VIM

#### **Description**:

This algorithm trains a linear Perceptron classifier with a margin by adjusting the weight step size.

#### Pseudo-code

**<u>begin initialize</u>** *a*, threshold  $\theta$ , margin *b*,  $\eta$ (.),  $k \leftarrow 0$ 

<u>do</u>  $k \leftarrow (k+1) \mod n$ <u>if</u>  $a^t y^k \le b$  <u>then</u>  $a \leftarrow a + \eta(k) y^k$ <u>until</u>  $a^t y^k > b$  for all k<u>return</u> a

<u>end</u>

### Syntax:

predicted\_targets = Perceptron\_VIM(training\_patterns, training\_targets, test\_patterns, input parameter);

[predicted\_targets, weights] = Perceptron\_VIM(training\_patterns, training\_targets, test\_patterns, input parameter);

## Additional inputs:

- 1. The margin *b*.
- 2. The maximum number of iterations.
- 3. The convergence criterion.
- 4. The convergence rate.

## Additional outputs:

The weight vector for the linear classifier.

## **Batch Variable Increment Perceptron**

Function name: Perceptron\_BVI

## **Description**:

This algorithm trains a linear Perceptron classifier in the batch mode, and where the learning rate is variable.

Pseudo-code:

**<u>begin initialize</u>**  $a, \eta(.), k \leftarrow 0$ 

$$\underline{do} \ k \leftarrow (k+1) \mod n$$

$$Y_k = \{ \}$$

$$j = 0$$

$$\underline{do} \ j \leftarrow j+1$$

$$\underline{if} \ \mathbf{y}_j \text{ is misclassified } \underline{then} \text{ Append } \mathbf{y}_j \text{ is to } Y_k$$

$$\underline{until} \ j = n$$

$$a \leftarrow a + n(k) \sum \mathbf{y}$$

$$a \leftarrow a + \eta(k) \sum_{y \in Y_k} y$$
  
until  $Y_k = \{\}$ 

<u>return</u> a

<u>end</u>

#### Program descriptions

## Syntax:

predicted\_targets = Perceptron\_BVI(training\_patterns, training\_targets, test\_patterns, input parameter);

[predicted\_targets, weights] = Perceptron\_BVI(training\_patterns, training\_targets, test\_patterns, input parameter);

## Input parameters:

Either the maximum number of iterations, or a weight vector for the training samples, or both.

## Additional outputs:

The weight vector for the linear classifier.

# **Balanced Winnow**

Function name: Balanced\_Winnow

#### **Description**:

This algorithm implements the balanced Winnow algorithm, which uses both a positive and negative weight vectors, each adjusted toward the final decision boundary from opposite sides.

### Pseudo-code:

**begin initialize**  $\mathbf{a}^+$ ,  $\mathbf{a}^-$ ,  $\eta(.)$ ,  $k \leftarrow 0$ ,  $\alpha > 1$  **if** Sgn[ $\mathbf{a}^{+t}\mathbf{y}_k - \mathbf{a}^{-t}\mathbf{y}_k$ ]  $| z_k$  (pattern misclassified) **then if**  $z_k = +1$  **then**  $a_i^{\dagger} \leftarrow \alpha^{y_i}a_i^{\dagger}$ ;  $a_i^- \leftarrow \alpha^{-y_i}a_i^{-}$  for all i **if**  $z_k = -1$  **then**  $a_i^{\dagger} \leftarrow \alpha^{-y_i}a_i^{\dagger}$ ;  $a_i^- \leftarrow \alpha^{y_i}a_i^{-}$  for all i**return**  $\mathbf{a}^+$ ,  $\mathbf{a}^-$ 

<u>end</u>

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#### Syntax:

predicted\_targets = Balanced\_Winnow(training\_patterns, training\_targets, test\_patterns, input parameters);

### Input parameters:

- 1. The maximum number of iterations.
- 2. The scaling parameter, alpha.
- 3. The convergence rate, eta.

## Additional outputs:

The positive weight vector and the negative weight vector.

## **Batch Relaxation with Margin**

Function name: Relaxation\_BM

**Description**: This algorithm trains a linear Perceptron classifier with margin *b* in the batch mode.

Pseudo-code:

```
begin initialize a, \eta(.), b, k \leftarrow 0

do k \leftarrow (k+1) mod n

Y_k = \{\}

j = 0

do j \leftarrow j + 1

if a^t y^j \le b then Append \mathbf{y}_j is to Y_k

until j = n

a \leftarrow a + \eta(k) \sum_{y \in Y_k} \frac{b - a^t y}{|y|^2}

until Y_k = \{\}

return a
```

end

#### Program descriptions

## Syntax:

predicted\_targets = Relaxation\_BM(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights] = Relaxation\_BM(training\_patterns, training\_targets, test\_patterns, input parameters);

## Input parameters:

- 1. The maximum number of iterations.
- 2. The target margin, *b*.
- 3. The convergence rate, eta.

## Additional outputs:

The weight vector for the final linear classifier.

## **Single-Sample Relaxation with Margin**

Function name: Relaxation SSM

## **Description**:

This algorithm trains a linear Perceptron classifier with margin on a per-pattern basis.

#### Pseudo-code

**begin initialize**  $a, b, \eta(.), k \leftarrow 0$ 

<u>**do**</u>  $k \leftarrow (k+1) mod n$ 

**if** 
$$a^t y^j \le b$$
 then  $a \leftarrow a + \eta(k) \frac{b - a^t y^k}{|y^k|^2} y^k$ 

**until** 
$$\mathbf{a}^{\mathsf{t}}\mathbf{y}^{\mathsf{k}} > b$$
 for all  $\mathbf{y}^{\mathsf{k}}$ 

<u>return</u> a

#### <u>end</u>

## Syntax:

predicted\_targets = Relaxation\_SSM(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights] = Relaxation\_SSM(training\_patterns, training\_targets, test\_patterns, input parameters);

## Input parameters:

- 1. The maximum number of iterations.
- 2. The margin, *b*.
- 3. The convergence rate, eta.

## Additional outputs:

The weight vector for the final linear classifier.

## **Least-Mean Square**

Function name: LMS

#### **Description**:

This algorithm trains a linear Perceptron classifier using the least-mean square algorithm.

#### Pseudo-code

**<u>begin initialize</u>** a, b, threshold  $\theta, \eta(.), k \leftarrow 0$ 

 $\underline{\mathbf{do}} \ k \leftarrow (k+1) \mod n$  $\mathbf{a} \leftarrow \mathbf{a} + \eta(k)(\mathbf{b}_k - \mathbf{a}^t \mathbf{y}^k) \mathbf{y}^k$  $\underline{\mathbf{until}} \ \left| \eta(k)(\mathbf{b}_k - \mathbf{a}^t \mathbf{y}^k) \right| < \theta$ 

#### <u>return</u> a

<u>end</u>

## Syntax:

predicted\_targets = LMS(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights] = LMS(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights, weights\_through\_the\_training] = LMS(training\_patterns, training\_targets, test\_patterns, input parameters);

## Input parameters:

- 1. The maximum number of iterations.
- 2. The convergence criterion.
- 3. The convergence rate.

## Additional outputs:

- 1. The final weight vector.
- 2. The weight vector throughout the training procedure.

## **Least-Squares Classifier**

Function name: LS

#### **Description**:

This algorithm trains a linear classifier by computing the weight vector using the Moore-Penrose pseudo-inverse, i.e.:

 $w = (PP^T)^{-1}PT^T$ 

where P is the pattern matrix and T the target vector.

## Syntax:

predicted\_targets = LS(training\_patterns, training\_targets, test\_patterns, input parameter);

[predicted\_targets, weights] = LS(training\_patterns, training\_targets, test\_patterns, input parameter);

## **Input parameters**:

An optional weight vector for weighted least squares.

## Additional outputs:

The weight vector of the final trained classifier.

# **Ho-Kashyap**

Function name: Ho\_Kashyap

## **Description**:

This algorithm trains a linear classifier by the Ho-Kashyap algorithm.

## Pseudo-code

## **Regular Ho-Kashyap**

**<u>begin initialize</u>**  $a, b, \eta(.) < 1$ , threshold  $b_{min}, k_{max}$ 

$$\begin{array}{l} \underline{do} \ k \leftarrow (k+1)mod \ n \\ e \leftarrow Ya - b \\ e^{\dagger} \leftarrow 1/2(e + Abs(e)) \\ b \leftarrow b + 2\eta(k)e^{\dagger} \\ a \leftarrow Y^{\dagger}b \\ \underline{if} \ Abs(e) \ \eth \ b_{min} \ \underline{then \ return} \ a, \ b \ \mathrm{and} \ \underline{exit} \\ \underline{until} \ k = k_{max} \end{array}$$

Print "NO SOLUTION FOUND"

<u>end</u>

**Modified Ho-Kashyap** 

**begin initialize**  $a, b, \eta < 1$ , threshold  $b_{min}, k_{max}$ 

 $\begin{array}{l} \underline{do} \ k \leftarrow (k+1)mod \ n \\ e \leftarrow Ya - b \\ e^{\dagger} \leftarrow 1/2(e + Abs(e)) \\ b \leftarrow b + 2\eta(k)(e + Abs(e)) \\ a \leftarrow Y^{\dagger}b \\ \underline{if} \ Abs(e) \ \eth \ b_{min} \ \underline{then} \ \underline{return} \ a, b \ \mathrm{and} \ \underline{exit} \\ \underline{until} \ k = k_{max} \end{array}$ 

Print "NO SOLUTION FOUND"

end

### Syntax:

predicted\_targets = Ho\_Kashyap(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights] = Ho\_Kashyap(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights, final\_margin] = Ho\_Kashyap(training\_patterns, training\_targets, test\_patterns, input parameters);

### Additional inputs:

- 1. The type of training (Basic or modified).
- 2. The maximum number of iterations.
- 3. The convergence criterion.
- 4. The convergence rate.

## Additional outputs:

- 1. The weights for the linear classifier.
- 2. The final computed margin.

# **Voted Perceptron Classifier**

Function name: Perceptron\_Voted

## **Description**:

The voted Perceptron is a variant of the Perceptron where, in this implementation, the data may be transformed using a kernel function so as to increase the separation between classes.

## Syntax:

predicted\_targets = Perceptron\_Voted(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

- 1. Number of perceptrons.
- 2. Kernel type: Linear, Polynomial, or Gaussian.
- 3. Kernel parameters.

# **Pocket Algorithm**

Function name: Pocket

#### **Description**:

The pocket algorithm is a simple modification over the Perceptron algorithm. The improvement is that updates to the weight vector are retained only if they perform better on a random sample of the data. In the current MAT-LAB implementation, the weight vector is trained for 10 iterations. Then, the new weight vector and the previous weight vector are used to train randomly selected training patterns. If the new weight vector succeeded in classifying more patterns before it misclassified a pattern compared to the old weight vector, the new weight vector replaces the old weight vector. The procedure is repeated until convergence or the maximum number of iterations is reached.

#### Syntax:

predicted\_targets = Pocket(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights] = Pocket(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

Either the maximal number of iterations or weight vector for the training samples, or both.

#### Additional outputs:

The weight vector for the final linear classifier.

## **Farthest-margin perceptron**

Function name: Perceptron FM

#### **Description**:

This algorithm implements a slight variation on the traditional Perceptron algorithm, with the only difference that the wrongly classified sample *farthest* from the current decision boundary is used to adjust the weight of the classifier.

#### Syntax:

predicted\_targets = Perceptron\_FM(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights] = Perceptron\_FM(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

- 1. The maximum number of iterations.
- 2. The slack for incorrectly classified examples

### Additional outputs:

The weight vector for the trained linear classifier.

# **Support Vector Machine**

Function name: SVM

#### **Description**:

This algorithm implements a support vector machine and works in two stages. In the first stage, the algorithm transforms the data by a kernel function; in the second stage, the algorithm finds a linear separating hyperplane in kernel space. The first stage depends on the selected kernel function and the second stage depends on the algorithmic solver method selected by the user. The solver can be a quadratic programming algorithm, a simple farthest-margin Perceptron, or the Lagrangian algorithm. The number of support vectors found will usually be larger than is actually needed if the first two solvers are used because both solvers are approximate.

#### Syntax:

predicted\_targets = SVM(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, alphas] = SVM(training\_patterns, training\_targets, test\_patterns, input parameters);

### Input parameters:

- 1. The kernel function: Gauss (or RBF), Poly, Sigmoid, or Linear.
- 2. Kernel parameter: For each kernel parameters the following parameters are needed:
- RBF kernel: Gaussian width (scalar parameter)
- Poly kernel: The integer degree of the polynomial
- Sigmoid: The slope and constant of the sigmoid
- Linear: no parameters are needed
- 3. The choice of solver: Perceptron, Quadprog, or Lagrangian.
- 4. The slack, or tolerance.

### Additional outputs:

The SVM coefficients.

# **Regularized Descriminant Analysis**

Function name: RDA

## **Description**:

This algorithm functions much as does the ML algorithm. However, once the mean and covariance of Gaussians are estimated they are shrunk.

## Syntax:

predicted\_targets = RDA(training\_patterns, training\_targets, test\_patterns, input parameter);

## Input parameter:

The shrinkage coefficient.

## **Reference:**

J. Friedman, "Regularized discriminant analysis," *Journal of the American Statistical Association*, **84**:165-75 (1989)

# Chapter 6

## **Stochastic Backpropagation**

Function name: Backpropagation\_Stochastic

#### **Description**:

This algorithm implements the stochastic backpropagation learning algorithm in a three-layer network of nonlinear units.

#### **Pseudo-code:**

**<u>begin initialize</u>**  $n_H$ , w, criterion  $\theta$ ,  $\eta$ ,  $m \leftarrow 0$ 

 $\frac{\mathbf{do}}{\mathbf{w}} = m \leftarrow m + 1$   $\mathbf{x}^{m} \leftarrow randomly \ chosen \ pattern$   $w_{ji} \leftarrow w_{ji} + \eta \delta_{j} x_{i} \ ; \ w_{kj} \leftarrow w_{kj} + \eta \delta_{k} y_{j}$   $\mathbf{until} \|\nabla J(\mathbf{w})\| < \theta$ 

<u>return</u> w

end

#### Syntax:

predicted\_targets = Backpropagation\_Stochastic(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who, errors\_throughout\_training] = Backpropagation\_Stochastic(training\_patterns, training\_targets, test\_patterns, input parameters);

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where:

Wih are the input-to-hidden unit weights

Who are the hidden-to-output unit weights

### **Input parameters:**

- 1. The number of hidden units  $n_{H}$ .
- 2. The convergence criterion  $\theta$ .
- 3. The convergence rate.

## Additional outputs:

- 1. The input-to-hidden weights  $w_{ji}$ .
- 2. The hidden-to-output weights  $w_{ki}$ .
- 3. The test errors through the training.

## Stochastic Backpropagation with momentum

Function name: Backpropagation\_SM

#### **Description**:

This algorithm implements the stochastic backpropagation learning algorithm in a three-layer network of nonlinear units with momentum.

#### **Pseudo-code:**

**<u>begin initialize</u>**  $n_H$ , w,  $\alpha$ (<1),  $\theta$ ,  $\eta$ ,  $m \leftarrow 0$ ,  $b_{ji} \leftarrow 0$ ,  $b_{kj} \leftarrow 0$ 

 $\begin{array}{l} \underline{do} \ m \leftarrow m+1 \\ & \mathbf{x}^m \leftarrow randomly \ chosen \ pattern \\ & b_{ji} \leftarrow \eta(1-\alpha)\delta_j x_i + \alpha b_{ji} \ ; \ b_{kj} \leftarrow \eta(1-\alpha)\delta_k y_j + \alpha b_{kj} \\ \\ & \underline{until} \ \|\nabla J(\mathbf{w})\| < \theta \end{array}$ 

<u>return</u> w

#### <u>end</u>

#### Syntax:

predicted\_targets = Backpropagation\_SM(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who] = Backpropagation\_SM(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who, errors\_throughout\_training] = Backpropagation\_SM(training\_patterns, training\_targets, test\_patterns, input parameters);

**Programs for Chapter 6** 

where:

Wih are the input-to-hidden unit weights

Who are the hidden-to-output unit weights

## Input parameters:

- 1. The number of hidden units  $n_{H}$ .
- 2. The convergence criterion  $\theta$ .
- 3. The convergence rate.

### Additional outputs:

- 1. The input-to-hidden weights  $w_{ii}$ .
- 2. The hidden-to-output weights  $w_{kj}$ .
- 3. The test errors through the training.

# **Batch Backpropagation**

Function name: Backpropagation\_Batch

### **Description**:

This algorithm implements the batch backpropagation learning algorithm in a three-layer network of nonlinear units.

### **Pseudo-code:**

**<u>begin initialize</u>**  $n_H$ , w, criterion  $\theta$ ,  $\eta$ ,  $r \leftarrow 0$ 

$$\begin{array}{ll} \underline{\mathbf{do}} & r \leftarrow r+1 \quad (\text{increment epoch}) \\ & m \leftarrow 0 \; ; \; \Delta w_{ji} \leftarrow 0 \; ; \; \Delta w_{kj} \leftarrow 0 \\ & \underline{\mathbf{do}} & m \leftarrow m+1 \\ & & \mathbf{x}^m \leftarrow select \; pattern \\ & & \Delta w_{ji} \leftarrow \Delta w_{ji} + \eta \delta_j x_i \; \; ; \; \Delta w_{kj} \leftarrow \Delta w_{kj} + \eta \delta_k y_j \\ & \underline{\mathbf{until}} \; m = n \\ & & w_{ji} \leftarrow w_{ji} + \eta \delta_j x_i \; ; \; w_{kj} \leftarrow w_{kj} + \eta \delta_k y_j \\ & \underline{\mathbf{until}} \; \| \nabla J(\mathbf{w}) \| < \theta \end{array}$$

<u>return</u> w

<u>end</u>

#### Syntax:

- predicted\_targets = Backpropagation\_Batch(training\_patterns, training\_targets, test\_patterns, input parameters);
- [predicted\_targets, Wih, Who] = Backpropagation\_Batch(training\_patterns, training\_targets, test\_patterns, input parameters);
- [predicted\_targets, Wih, Who, errors\_throughout\_training] = Backpropagation\_Batch(training\_patterns, training\_targets, test\_patterns, input parameters);

#### where:

Wih are the input-to-hidden unit weights

Who are the hidden-to-output unit weights

#### **Input parameters:**

- 1. The number of hidden units  $n_H$ .
- 2. The convergence criterion  $\theta$ .
- 3. The convergence rate.

## Additional outputs:

- 1. The input-to-hidden weights  $w_{ji}$ .
- 2. The hidden-to-output weights  $w_{kj}$ .
- 3. The training and test errors through the training.
# **Backpropagation trained using Conjugate Gradient Descent**

Function name: Backpropagation\_CGD

#### **Description**:

This algorithm trains a three-layer network of nonlinear units using conjugate gradient descent (CGD). CGD usually helps the network converge faster than first order methods.

#### Syntax:

predicted\_targets = Backpropagation\_CGD(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who] = Backpropagation\_CGD(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who, errors\_throughout\_training] = Backpropagation\_CGD(training\_patterns, training\_targets, test\_patterns, input parameters);

where:

Wih are the input-to-hidden unit weights

Who are the hidden-to-output unit weights

# Input parameters:

- 1. The number of hidden units,  $n_H$ .
- 2. The convergence criterion  $\theta$ .

- 1. The input-to-hidden weights  $w_{ii}$ .
- 2. The hidden-to-output weights  $w_{ki}$ .
- 3. The training error through the training.

# **Recurrent Backpropagation**

Function name: Backpropagation\_Recurrent

**Description**: This algorithm trains a three-layer network of nonlinear units having recurrent connections. The network is fed with the inputs, and these are propagated until the network stabilizes. Then the weights are changed just as in traditional feed-forward networks.

#### Syntax:

predicted\_targets = Backpropagation\_Recurrent(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights] = Backpropagation\_Recurrent(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, weights, errors\_throughout\_training] = Backpropagation\_Recurrent(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

- 1. The number of hidden units,  $n_H$ .
- 2. The convergence criterion  $\theta$ .
- 3. The convergence rate.

- 1. The connection weights.
- 2. The errors through the training.

# **Cascade-Correlation**

Function name: Cascade Correlation

Description: This algorithm trains a nonlinear cascade-correlation neural network.

Pseudo-code

**begin initialize** *a*, criterion  $\theta$ ,  $\eta$ ,  $k \leftarrow 0$  **do**  $m \leftarrow m + 1$   $w_{ki} \leftarrow w_{ki} - \eta \nabla J(w)$  **until**  $\|\nabla J(w)\| < \theta$  **if**  $J(w) > \theta$  **then** add hidden unit **until exit do**  $m \leftarrow m + 1$   $w_{ji} \leftarrow w_{ji} - \eta \nabla J(w)$ ;  $w_{kj} \leftarrow w_{kj} - \eta \nabla J(w)$  **until**  $\|\nabla J(w)\| < \theta$ **return** *w* 

end

#### Syntax:

predicted\_targets = Cascade\_Correlation(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who] = Cascade\_Correlation(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who, errors\_throughout\_training] = Cascade\_Correlation(training\_patterns,

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training\_targets, test\_patterns, input parameters);

where:

Wih are the input-to-hidden unit weights

Who are the hidden-to-output unit weights

## **Input parameters**:

- 1. The convergence criterion  $\theta$ .
- 2. The convergence rate.

- 1. The input-to-hidden weights  $w_{ii}$ .
- 2. The hidden-to-output weights  $w_{kj}$ .
- 3. The training error through the training.

# **Optimal Brain Surgeon**

Function name: Optimal\_Brain\_Surgeon

### **Description**:

This algorithm prunes a trained three-layer network by means of Optimal Brain Surgeon or Optimal Brain Damage.

#### Pseudo-code:

### <u>begin initialize</u> $n_H$ , a, $\theta$

train a reasonably large network to minimum error

**<u>do</u>** compute  $H^{-1}$  (inverse Hessian matrix)

$$q^* \leftarrow \arg min_q \frac{w_q^2}{2[H^{-1}]_{qq}} \text{ (saliency } L_q)$$

$$\boldsymbol{w} \leftarrow \boldsymbol{w} - \frac{\boldsymbol{w}_{q^*}}{[\boldsymbol{H}^{-1}]_{q^*q^*}} \boldsymbol{H}^{-1} \boldsymbol{e}_{q^*}$$

<u>until</u>  $J(w) > \theta$ 

<u>return</u> w

<u>end</u>

#### Syntax:

predicted\_targets = Optimal\_Brain\_Surgeon(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who] = Optimal\_Brain\_Surgeon(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who, errors\_throughout\_training] = Optimal\_Brain\_Surgeon(training\_patterns, training\_targets, test\_patterns, input parameters);

where:

Wih are the input-to-hidden unit weights

Who are the hidden-to-output unit weights

### Input parameters:

1. The initial number of hidden units.

2. The convergence rate.

- 1. The input-to-hidden weights  $w_{ii}$ .
- 2. The hidden-to-output weights  $w_{ki}$ .
- 3. The training error through the training.

# Quickprop

Function name: Backpropagation\_Quickprop

#### **Description**:

This algorithm trains a three-layer network by means of the Quickprop algorithm.

#### Syntax:

predicted\_targets = Backpropagation\_Quickprop(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who] = Backpropagation\_Quickprop(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, Wih, Who, errors\_throughout\_training] = Backpropagation\_Quickprop(training\_patterns, training\_targets, test\_patterns, input parameters);

where: Wih are the input-to-hidden unit weights Who are the hidden-to-output unit weights

## Input parameters:

- 1. The number of hidden units  $n_H$ .
- 2. The convergence criterion.
- 3. The convergence rate.
- 4. The error correction rate.

- 1. The input-to-hidden weights  $w_{ji}$ .
- 2. The hidden-to-output weights  $w_{ki}$ .
- 3. The training error through the training.

# **Projection Pursuit**

Function name: Projection\_Pursuit

#### **Description**:

This algorithm implements the projection pursuit statistical estimation procedure.

## Syntax:

predicted\_targets = Projection\_Pursuit(training\_patterns, training\_targets, test\_patterns, input parameter);

[predicted\_targets, component\_weights, output\_weights] = Projection\_Pursuit(training\_patterns, training\_targets, test\_patterns, input parameter);

#### Input parameters:

The number of component features onto which the data is projected.

- 1. The component weights.
- 2. The output unit weights

# **Radial Basis Function Classifier**

Function name: RBF Network

#### **Description**:

This algorithm trains a radial basis function classifier. First the algorithm computes the centers for the data using k-means. Then the algorithm estimates the variance of the data around each center, and uses this estimate to compute the activation of each training pattern to these centers. These activation patterns are used for computing the gating unit of the classifier, via the Moore-Penrose pseudo-inverse.

#### Syntax:

predicted\_targets = RBF\_Network(training\_patterns, training\_targets, test\_patterns, input parameter);

[predicted\_targets, component\_weights, output\_weights] = RBF\_Network(training\_patterns, training\_targets, test\_patterns, input parameter);

#### Input parameter:

The number of hidden units.

- 1. The locations in feature space of the centers of the hidden units.
- 2. The weights of the gating units.

Chapter 7

# **Stochastic Simulated Annealing**

Function name: Stochastic\_SA

**Description**: This algorithm clusters the patterns using stochastic simulated annealing in a network of binary units.

#### **Pseudo-code:**

**<u>begin initialize</u>** T(k),  $k_{max}$ ,  $s_i(1)$ ,  $w_{ij}$  for i, j = 1, ..., N

 $k \leftarrow 0$ 

**<u>do</u>**  $k \leftarrow k + 1$ 

**<u>do</u>** select node *i* randomly; suppose its state is  $s_i$ 

$$E_{a} \leftarrow -1/2 \sum_{j}^{N_{i}} w_{ij} s_{i} s_{j}$$

$$E_{b} \leftarrow -E_{a}$$
**if**  $E_{b} < E_{a}$ 
**then**  $s_{i} \leftarrow -s_{i}$ 
**else if**  $e^{-\frac{(E_{b} - E_{a})}{T(k)}} > Rand[0, 1]$ 
**then**  $s_{i} \leftarrow -s_{i}$ 

until all nodes polled several times

**<u>until</u>**  $k = k_{max}$  or stopping criterion met

**<u>return</u>** *E*,  $s_i$ , for i = 1, ..., N

#### <u>end</u>

## Syntax:

[new\_patterns, new\_targets] = Stochastic\_SA(training\_patterns, training\_targets, input\_parameters, plot\_on);

#### **Input parameters**:

- 1. The number of output data points.
- 2. The cooling rate.

The input flag *plot\_on* determines if the algorithm's progress should be shown through the learning iterations.

# **Deterministic Simulated Annealing**

Function name: Deterministic\_SA

#### **Description**:

This algorithm clusters the data using deterministic simulated annealing in a network of binary units.

#### Pseudo-code

**begin initialize** T(k),  $w_{ij}$ ,  $s_i(1)$  for i, j = 1, ... N

 $k \leftarrow 0$ 

 $\underline{\mathbf{do}}\ k \leftarrow k+1$ 

select node *i* randomly

$$l_i \leftarrow \sum_{j}^{N_i} w_{ij} s_j$$
$$s_i \leftarrow f(l_i, T(k))$$

**<u>until</u>**  $k = k_{max}$  or stopping criterion met

**<u>return</u>** *E*,  $s_i$ , for i = 1, ..., N

end

#### Syntax:

[new\_patterns, new\_targets] = Stochastic\_SA(training\_patterns, training\_targets, input\_parameters, plot\_on);

## Input parameters:

- 1. The number of output data points.
- 2. The cooling rate.

The input flag *plot\_on* determines if the algorithm's progress should be shown through the learning iterations.

# **Deterministic Boltzmann Learning**

Function name: BoltzmannLearning

Description: Use deterministic Bolzmann learning to find a good combination of weak learners to classify data.

Pseudo-code

**<u>begin initialize</u>** D,  $\eta$ , T(k),  $w_{ij}$  for i, j = 1, ... N

<u>do</u> randomly select training pattern x

randomize states  $s_i$ 

anneal network with input and output clamped

at final, low *T*, calculate  $[s_i s_j]_{\alpha^i \alpha^o clamped}$ 

randomize states  $s_i$ 

anneal network with input clamped but output free

at final, low *T*, calculate  $[s_i s_j]_{\alpha^i clamped}$ 

 $w_{ij} \leftarrow w_{ij} + (\eta/T) [[s_i s_j]_{\alpha^i \alpha^o clamped} - [s_i s_j]_{\alpha^i clamped}]$ 

**<u>until</u>**  $k = k_{max}$  or stopping criterion met

return w<sub>ij</sub>

end

#### Syntax:

predicted\_targets = Deterministic\_Boltzmann(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

- 1. The number of input units.
- 2. The number of hidden units.
- 3. The cooling rate.
- 4. The type of weak learner.
- 5. The parameters of the weak learner.

#### Additional outputs:

The errors during training.

# **Basic Genetic Algorithm**

Function name: Genetic\_Algorithm

#### **Description**:

This implementation uses a basic genetic algorithm to build a classifier from components of weak classifiers.

#### Pseudo-code

**begin initialize**  $\theta$ ,  $P_{co}$ ,  $P_{mut}$ , L *N*-bit chromosomes

**<u>do</u>** determine the fitness of each chromosome  $f_i$ , i = 1, ..., L

rank the chromosomes

do select two chromosomes with the highest score

<u>**if**</u> Rand $[0,1) < P_{co}$  <u>**then**</u> crossover the pair at a randommly chosen bit

<u>else</u> change each bit with proability  $P_{mut}$ ;

remove the parent chromosomes

until N offspring have been created

**<u>until</u>** any chromosome's score f exceeds  $\theta$ 

return highest fitness chromosome (best classifier)

end

## Syntax:

predicted\_targets = Genetic\_Algorithm(training\_patterns, training\_targets, test\_patterns, input parameters);

### **Input parameters**:

- 1. The probability of cross-over  $P_{co}$ .
- 2. The probability of mutation  $P_{mut}$ .
- 3. The type of weak classifier.
- 4. The parameters of the weak learner.
- 5. The target or stopping error on training set.
- 6. The number of solutions to be returned by the program.

# **Genetic Programming**

Function name: Genetic\_Programming

**Description**: This algorithm approximates a function by evolving mathematical expressions by a genetic programming algorithm. The function is used to classify the data.

## Syntax:

predicted\_targets = Genetic\_Programming(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, best\_function\_found] = Genetic\_Programming(training\_patterns, training\_targets, test\_patterns, input parameters);

### Input patterns:

- 1. The initial function length.
- 2. The number of generations.
- 3. The number of solutions to be returned by the program.

#### Additional outputs:

The best function found by the algorithm.

# Chapter 8

# C4.5

Function name: C4\_5

### **Description**:

Construct a decision tree recursively so as to minimize the error on a training set. Discrete features are split using a histogram and continuous features are split using an information criteria. The algorithm is implemented under the assumption that a pattern vector with fewer than 10 unique values is discrete, and will be treated as such. Other vectors are treated as continuous. Note that due to MATLAB memory and processing restrictions, the recursion depth may be reached during the processing of a large complicated data set, which will result in an error.

### Syntax:

predicted\_targets = C4\_5(training\_patterns, training\_targets, test\_patterns, input parameter);

#### Input parameter:

The maximum percentage of error at a node that will prevent it from further splitting.

# CART

Function name: CART

### Description:

Construct a decision tree recursively so as to minimize the error on a training set. The criterion for splitting a node is either the percentage of incorrectly classified samples at the node, or the entropy at the node, or the variance of the outputs. Note that due to MATLAB memoery and processing restrictions, the recursion depth may be reached during the processing of a large complicated data set, which will result in an error.

### Syntax:

predicted\_targets = CART(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

- 1. The splitting criterion (entropy, variance, or misclassification).
- 2. Maximum percentage of incorrectly assigned samples at a node.

# ID3

Function name: ID3

#### Description:

Construct a decision tree recursively so as to minimize the error on a training set. This algorithm assumes that the data takes discrete values. The criterion for splitting a node is the percentage of incorrectly classified samples at the node. Note that due to MATLAB memoery and processing restrictions, the recursion depth may be reached during the processing of a large complicated data set, which will result in an error.

#### Syntax:

predicted\_targets = ID3(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

1. Maximum number of values the data can take (i.e. the number of values that the data will be binned into).

2. Maximum percentage of incorrectly assigned samples at a node.

# **Naive String Matching**

Function name: Naive\_String\_Matching

#### **Description:**

Perform naive string matching, which is quite inefficient in the general case. The value of this program is primarily for making performance comparisons with the Boyer-Moore algorithm. Note that this algorithm is in the "Other" directory.

#### Pseudo-code

#### **begin initialize** A, $a, n \leftarrow \text{length}[text], m \leftarrow \text{length}[x]$

 $s \leftarrow 0$ 

<u>while</u> s < n - m

 $\underline{\mathbf{if}} \mathbf{x}[1...m] = text[s+1...s+m]$ 

then print "pattern occurs at shift" s

 $s \leftarrow s+1$ 

<u>return</u>

end

Syntax:

location = Naive\_String\_Matching(text\_vector, search\_string);

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# **Boyer-Moor String Matching**

Function name: Boyer\_Moore\_string\_matching

#### **Description**:

Perform string matching by the Boyer-Moore algorithm, which is typically far more efficient than naive string matching. Note that this algorithm is in the "Other" directory.

#### Pseudo-code

**begin initialize** A,  $a, n \leftarrow \text{length}[text], m \leftarrow \text{length}[x]$ 

 $F(x) \leftarrow \text{last-occurrence function}, \ \Im(x) \leftarrow \text{good-suffix function}$ 

 $s \leftarrow 0$  **while**  $s \eth n - m$  **do**  $j \leftarrow m$  **while** j > 0 and  $\mathbf{x}[j] = text[s+j]$  **do**  $j \leftarrow j - 1$  **if** j = 0 **then** print "pattern occurs at shift" s  $s \leftarrow s + G(0)$  **else**  $s \leftarrow s + max[G(j), j - F(text[s+j])]$ 

#### <u>return</u>

#### <u>end</u>

#### Syntax:

location = Naive\_String\_Matching(text\_vector, search\_string);

# **Edit Distance**

Function name: Edit\_Distance

## **Description**:

Compute the edit distance between two strings x and y. Note that this algorithm is in the "Other" directory.

#### Pseudo-code

**<u>until</u>** i = m**<u>return</u> C**[m,n]

<u>end</u>

Syntax:

distance\_matrix = Edit\_Distance(text\_vector1, text\_vector2);

# **Bottom-Up Parsing**

Function name: Bottom\_Up\_Parsing

#### **Description**:

Perform bottom-up parsing of a string x in grammar G. Note that this algorithm is in the "Other" directory.

#### Pseudo-code

```
begin initialize G = (A, I, S, P), \mathbf{x} = x_I x_2 \dots x_n

i \leftarrow 0

do i \leftarrow i + 1

V_{i1} \leftarrow \{A | A \rightarrow x_i\}

mtil i = n

j \leftarrow 1

do j \leftarrow j + 1

i \leftarrow 0

do i \leftarrow i + 1

V_{ij} \leftarrow \emptyset

k \leftarrow 0

do k \leftarrow k + 1

V_{ij} \leftarrow V_{ij} \cup \{A | A \rightarrow BC \in P, B \in V_{ik} \text{and} C \in V_{i+k,j-k}\}

mtil k = j - 1
```

<u>**until**</u> *i* = *n* - *j* + 1

**<u>until</u>** j = n

**<u>if</u>**  $S \in V_{1n}$  **<u>then</u>** *print* "parse of" x "successful in G"

# <u>return</u>

<u>end</u>

# Syntax:

parsing\_table = Bottom\_Up\_Parsing(alphabet\_vector, variable\_vector, root\_symbol, production\_rules, text\_vector);

# **Grammatical Inference (Overview)**

Function name: Grammatical\_Inference

#### **Description**:

Infers a grammar G from a set of positive and negative example strings and a (simple) initial grammar  $G^0$ . Note that this algorithm is in the "Other" directory.

#### Pseudo-code

 begin initialize D<sup>+</sup>,D<sup>-</sup>,G<sup>0</sup>

  $n^{\dagger} \leftarrow |D^{\dagger}|$  (number of instances in D<sup>+</sup>)

  $S \leftarrow S$ 
 $A \leftarrow$  set of characters in D<sup>+</sup>

  $i \leftarrow 0$ 
**do**  $i \leftarrow i + 1$  

 read  $x_i^{+}$  from D<sup>+</sup>

 **if**  $x_i^{+}$  cannot be parsed by G

 **then do** propose additional productions to P and variables to I

 accept updates if G parses  $x_i^{+}$  but no string in D<sup>-</sup>

 **until**  $i = n^+$  

 eliminate redundant productions

 **return**  $G \leftarrow \{A, I, S, P\}$ 

end

# Syntax:

[alphabet\_vector, variable\_vector, root\_symbol, production\_rules] = Grammatical\_Inference (text\_vectors\_to\_parse, labels);

# Chapter 9

# AdaBoost

Function name: Ada\_Boost

### **Description**:

AdaBoost builds a nonlinear classifier by constructing an ensemble of "weak" classifiers (i.e., ones that need perform only slightly better than chance) so that the joint decision is has better accuracy on the training set. It is possible to iteratively add classifiers so as to attain any given accuracy on the training set. In AdaBoost each sample of the training set is selected for training the weak with a probability proportional to how well it is classified. An incorrectly classified sample will be chosen more frequently for the training, and will thus be more likely to be correctly classified by the new weak classifier.

### Pseudo-code

**begin initialize** 
$$D = \{x^{1}, y_{1}, ..., x^{n}, y_{n}\}, k_{max}, W_{1}(i) = 1/n, i = 1, ..., n$$

$$k \leftarrow 0$$

 $\underline{\mathbf{do}} \ k \leftarrow k+1$ 

train weak learner  $C_k$  using D sampled according to  $W_k(i)$ 

 $E_k \leftarrow$  training error of  $C_k$  measured on D using  $W_k(i)$ 

$$\alpha_k \leftarrow \frac{1}{2} \ln\left[(1 - E_k)/E_k\right]$$
$$W_{k+1}(i) \leftarrow \frac{W_k(i)}{Z_k} \times \begin{cases} e^{-\alpha_k} ifh_k(\mathbf{x}^i) = y_i \\ e^{\alpha_k} ifh_k(\mathbf{x}^i) \neq y_i \end{cases}$$

<u>**until**</u>  $k = k_{max}$ 

**<u>return</u>**  $C_k$  and  $\alpha_k$  for k = 1 to  $k_{max}$  (ensemble of classifiers with weights)

### <u>end</u>

### Syntax:

predicted\_targets = Ada\_Boost(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, training\_errors] = Ada\_Boost(training\_patterns, training\_targets, test\_patterns, input parameters);

## Input parameters:

- 1. The number of boosting iterations.
- 2. The name of weak learner.
- 3. The parameters of the weak learner.

## Additional outputs:

The training errors throughout the learning.

# Local boosting

Function name: LocBoost

#### **Description**:

Create a single nonlinear classifier based on boosting of localized classifiers. The algorithm assigns local classifiers to incorrectly classified training data, and optimizes these local classifiers to reach the minimum error.

#### Syntax:

predicted\_targets = LocBoost(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

- 1. The number of boosting iterations.
- 2. The number of EM iterations.
- 3. The number of optimization steps.
- 4. The type of weak learner.
- 5. The weak learner parameters.

#### Reference

R. Meir, R. El-Yaniv and S. Ben-David, "Localized boosting," *Proceedings of the 13th Annual Conference on Computational Learning Theory* 

# **Bayesian Model Comparison**

Function name: Bayesian\_Model\_Comparison

#### **Description**:

Bayesian model comparison, as implemented here, selects the best mixture of Gaussians model for the data. Each full candidate model is constructed using Expectation-Maximization. The program then computes the Occam factor and finally returns the model that maximizes the Occam factor.

#### Syntax:

predicted\_targets = Bayesian\_Model\_Comparison(training\_patterns, training\_targets, test\_patterns, input parameters);

Input parameters: Maximum number of Gaussians for each models.

# **Component Classifiers with Discriminant Functions**

Function name: Components\_with\_DF

#### Description:

This implementation uses logistic component classifiers and a softmax gating function to create a global classifier. The parameters of the components are learned using Newton descent, and the parameters of the gating system using gradient descent.

#### Syntax:

```
predicted_targets = Components_with_DF(training_patterns, training_targets, test_patterns, input parameters);
```

[predicted\_targets, errors] = Components\_with\_DF(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

The component classifiers as pairs of classifier name and classifier parameters.

#### Additional outputs:

The errors through the training.
# **Component Classifiers without Discriminant Functions**

Function name: Components\_without\_DF

**Description**: This program works with any of the classifiers in the toolbox as components to build a single metaclassifier. The gating unit parameters are learned through gradient descent.

#### Syntax:

predicted\_targets = Components\_without\_DF(training\_patterns, training\_targets, test\_patterns, input parameters);

[predicted\_targets, errors] = Components\_without\_DF(training\_patterns, training\_targets, test\_patterns, input parameters);

#### Input parameters:

The component classifiers as pairs of classifier name and classifier parameters.

#### Additional outputs:

The errors through the training.

# ML\_II

Function name: ML\_II

### **Description**:

This algorithm finds the best multiple Gaussian model for the data, and uses this model to construct a decision surface. The algorithm computes the Gaussian parameters for the data via the EM algoritm, assuming varying number of Gaussians. Then, the algorithm computes the probability that the data was generated by these models and returns the most likely such model. Finally, the algorithm uses the parameters of this model to construct the Bayes decision region.

## Syntax:

predicted\_targets = ML\_II(training\_patterns, training\_targets, test\_patterns, input parameter);

## Input parameters:

Maximum number of Gaussians components per class.

# **Interactive Learning**

Function name: Interactive\_Learning

#### **Description**:

This algorithm implements interactive learning in a particular type of classifer, specifically, the nearest-neighbor interpolation on the training data. The training points that have the highest ambiguity are referred to the user for labeling, and each such label is used for improving the classification.

#### Syntax:

predicted\_targets = Interactive\_Learning(training\_patterns, training\_targets, test\_patterns, input parameters);

#### **Input parameters:**

- 1. The number of points presented as queries to the user.
- 2. The weight of each queried point relative the other data points.

# Chapter 10

# k-Means Clustering

Function name: K\_means

# **Description**:

This is a top-down clustering algorithm which attempts to find the c representative centers for the data. The initial means are selected from the training data itself. k-means is biased towards spherical clusters with similar variances.

## Pseudo-code

**begin initialize** *n*, *c*,  $\mu_1$ ,  $\mu_2$ , ...,  $\mu_c$ 

**<u>do</u>** classify *n* samples according to nearest  $\mu_i$ 

recompute  $\mu_i$ 

**<u>until</u>** no change in  $\mu_i$ 

<u>**return**</u>  $\mu_1, \mu_2, ..., \mu_c$ 

<u>end</u>

#### **Program descriptions**

[clusters, cluster\_labels] = k\_means(patterns, targets, input\_parameter, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = k\_means(patterns, targets, input\_parameter, plot\_on);

## Input parameter:

The number of desired output clusters, *c*.

The input parameter plot\_on determines if the cluster centers are plotted during training.

### Additional outputs:

# Fuzzy k-Means Clustering

Function name: fuzzy\_k\_means

#### Description:

This is a top-down clustering algorithm which attempts to find the k representative centers for the data. The initial means are selected from the training data itself. This algorithm uses a slightly different gradient search than the simple standard k-means algorithm, but generally yields the same final solution.

#### Pseudo-code

```
begin initialize n, c, b, \mu_I, \mu_2, ..., \mu_c, \hat{P}(\omega_i | \mathbf{x}_j), i = 1, ..., c; j = 1, ..., n
normalize \hat{P}(\omega_i | \mathbf{x}_j)
do recompute \mu_i
```

recompute  $\hat{P}(\omega_i | \mathbf{x}_j)$  **<u>until</u>** small change in  $\mu_I$  and  $\hat{P}(\omega_i | \mathbf{x}_j)$ <u>return</u>  $\mu_I$ ,  $\mu_2$ , ...,  $\mu_c$ 

end

#### **Program descriptions**

## Syntax:

[clusters, cluster\_labels] = fuzzy\_k\_means(patterns, targets, input\_parameter, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = fuzzy\_k\_means(patterns, targets, input\_parameter, plot\_on);

# Input parameter:

The number of desired output clusters, c.

The input parameter plot\_on determines if the cluster centers are plotted during training.

## Additional outputs:

# Kernel k-Means Clustering

Function name: kernel\_k\_means

#### **Description**:

This is a top-down clustering algorithm which is identical to the k-means algorithm (See above), except that the data is first mapped to a new space using a kernel function.

### Syntax:

[clusters, cluster\_labels] = kernel\_k\_means(patterns, targets, input\_parameter, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = kernel\_k\_means(patterns, targets, input\_parameter, plot\_on);

### Input parameters:

- 1. The number of desired output clusters, c.
- 2. The kernel function: Gauss (or RBF), Poly, Sigmoid, or Linear.
- 3. Kernel parameter: For each kernel parameters the following parameters are needed:
- RBF kernel: Gaussian width (scalar parameter)
- Poly kernel: The integer degree of the polynomial
- Sigmoid: The slope and constant of the sigmoid
- Linear: no parameters are needed

The input parameter plot\_on determines if the cluster centers are plotted during training.

### Additional outputs:

# Spectral k-Means Clustering

Function name: spectral k means

#### Description:

This is a top-down clustering algorithm which is identical to the k-means algorithm (See above), except that the data is first mapped to a new space using a kernel function and the clustering is performed in that space.

#### Syntax:

[clusters, cluster\_labels] = spectral\_k\_means(patterns, targets, input\_parameter, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = spectral\_k\_means(patterns, targets, input\_parameter, plot\_on);

#### Input parameters:

- 1. The number of desired output clusters, c.
- 2. The kernel function: Gauss (or RBF), Poly, Sigmoid, or Linear.
- 3. Kernel parameter: For each kernel parameters the following parameters are needed:
- RBF kernel: Gaussian width (scalar parameter)
- Poly kernel: The integer degree of the polynomial
- Sigmoid: The slope and constant of the sigmoid
- Linear: no parameters are needed
- 4. Clutering type: The clustering type can be:
- Multicut
- NJW (According to the method proposed by Ng, Jordan, and Weiss)

The input parameter plot\_on determines if the cluster centers are plotted during training.

#### Additional outputs:

# **Basic Iterative Minimum-Squared-Error Clustering**

Function name: **BIMSEC** 

#### Description:

This algorithm iteratively searches for the c clusters that minimize the sum-squared error of the training data with respect to the nearest cluster center. The initial clusters are selected from the data itself.

#### **Pseudo-code:**

begin initialize  $n, c, m_1, m_2, ..., m_c$ 

**<u>do</u>** randomly select a sample  $\hat{x}$ 

 $i \leftarrow \arg min_i \| \boldsymbol{m}_i - \hat{\boldsymbol{x}} \|$  (classify  $\hat{\boldsymbol{x}}$ )

<u>**if**</u>  $n_i / 1$  <u>**then**</u> compute

$$\rho_{j} = \begin{cases} \frac{n_{j}}{n_{j}+1} \left\| \hat{\boldsymbol{x}} - \boldsymbol{m}_{j} \right\|^{2} & j \neq i \\ \frac{n_{j}}{n_{j}-1} \left\| \hat{\boldsymbol{x}} - \boldsymbol{m}_{j} \right\|^{2} & j = i \end{cases}$$

**<u>if</u>**  $\rho_k < \rho_j$  for all j **<u>then</u>** transfer  $\hat{x}$  to  $D_k$ 

recompute  $J_{e}$ ,  $m_i$ ,  $m_k$ 

**<u>until</u>** no change in  $J_e$  in n attempts

<u>return</u>  $m_1, m_{2i}, ..., m_c$ 

end

#### Program descriptions

## Syntax:

[clusters, cluster\_labels] = BIMSEC(patterns, targets, input\_parameter, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = BIMSEC(patterns, targets, input\_parameter, plot\_on);

### Input parameter:

The number of desired output clusters, *c*.

The input parameter plot\_on determines if the cluster centers are plotted during training.

### Additional outputs:

# **Agglomerative Hierarchical Clustering**

### Function name: AGHC

### **Description**:

This function implements the bottom-up clustering. The algorithm starts by assuming each training point is its own cluster and then iteratively merges the nearest such clusters (where proximity is computed by a distance function) until the desired number of clusters are formed.

#### Pseudo-code

**<u>begin initialize</u>** c,  $\hat{c} \leftarrow n$ ,  $D_i \leftarrow \{x_i\}$ , i = 1, ..., n

 $\underline{\mathbf{do}} \ \hat{c} \leftarrow \hat{c} - 1$ 

find nearest clusters, say,  $D_i$  and  $D_i$ 

merge  $D_i$  and  $D_j$ 

**<u>until</u>**  $c = \hat{c}$ 

return c clusters

<u>end</u>

#### Program descriptions

## Syntax:

[clusters, cluster\_labels] = AGHC(patterns, targets, input\_parameters, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = AGHC(patterns, targets, input\_parameters, plot\_on);

## Input parameters:

- 1. The number of desired output clusters, c.
- 2. The type of distance function to be used (min, max, avg, or mean).

The input parameter plot\_on determines if the cluster centers are plotted during training.

#### Additional outputs:

# **Stepwise Optimal Hierarchical Clustering**

## Function name: SOHC

# **Description**:

This function implements the bottom-up clustering. The algorithm starts by assuming each training point is its own cluster and then iteratively merges the two clusters that change a clustering criterion the least, until the desired number of clusters c are formed.

## **Pseudo-code:**

**<u>begin initialize</u>** *c*,  $\hat{c} \leftarrow n$ ,  $D_i \leftarrow \{x_i\}$ , i = 1, ..., n

 $\underline{\mathbf{do}}\ \hat{c} \leftarrow \hat{c} - 1$ 

find clusters whose merger changes the criterion the least, say,  $D_i$  and  $D_i$ 

merge  $D_i$  and  $D_j$ 

**<u>until</u>**  $c = \hat{c}$ 

return c clusters

<u>end</u>

#### Program descriptions

## Syntax:

[clusters, cluster\_labels] = SOHC(patterns, targets, input\_parameter, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = SOHC(patterns, targets, input\_parameter, plot\_on);

## Input parameter:

The number of desired output clusters, *c*.

The input parameter plot\_on determines if the cluster centers are plotted during training.

#### Additional outputs:

# **Competitive Learning**

Function name: Competitive learning

### **Description**:

This function implements competitive learning clustering, where the nearest cluster center is updated according to the position of a randomly selected training pattern.

#### Pseudo-code

**begin initialize**  $\eta$ , *n*, *c*, *k*,  $w_1$ , ...,  $w_c$ 

 $\begin{aligned} \mathbf{x}_i \leftarrow \{1, \mathbf{x}_i\}, \ i = 1, ..., n \quad (\text{augment all patterns}) \\ \mathbf{x}_i \leftarrow \mathbf{x}_i / \|\mathbf{x}_i\|, \ i = 1, ..., n \quad (\text{normalize all patterns}) \\ j \leftarrow \arg\max_j \mathbf{w}_j^{\ t} \mathbf{x} \quad (\text{classify } \mathbf{x}) \\ \mathbf{w}_j \leftarrow \mathbf{w}_j + \eta \mathbf{x} \quad (\text{weight update}) \\ \mathbf{w}_j \leftarrow \mathbf{w}_j / \|\mathbf{w}_j\| \quad (\text{weight normalization}) \\ \underline{\mathbf{until}} \text{ no significant change in } \mathbf{w} \text{ in } k \text{ attempts} \end{aligned}$ 

<u>**return**</u>  $w_1, \ldots, w_c$ 

<u>end</u>

#### Program descriptions

### Syntax:

[clusters, cluster\_labels] = Competitive\_Learning(patterns, targets, input\_parameters, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = Competitive\_Learning(patterns, targets, input\_parameters, plot\_on);

[clusters, cluster\_labels, original\_data\_labels, weights] = Competitive\_Learning(patterns, targets, input\_parameters, plot\_on);

# Input parameters:

- 1. The number of desired output clusters, c.
- 2. The learning rate.

The input parameter plot\_on determines if the cluster centers are plotted during training.

# Additional outputs:

- 1. The number of the cluster assigned to each input pattern.
- 2. The weight matrix representing the cluster centers.

# **Basic Leader-Follower Clustering**

Function name: Leader\_Follower

### **Description**:

This function implements basic leader-follower clustering, which is similar to competitive learning but additionally generates a new cluster center whenever a new input pattern differs by more than a threshold distance  $\theta$  from existing clusters.

#### Pseudo-code

begin initialize $\eta, \theta$  $w_1 \leftarrow x$  $\underline{do}$  accept new x $j \leftarrow \arg max_j ||x - w_j||$  (find nearest cluster) $\underline{if} ||x - w_j|| < \theta$  $\underline{then} |w_j \leftarrow w_j + \eta x$  $\underline{else}$  add new  $w \leftarrow x$  $w \leftarrow w/||w||$  (normalize weight) $\underline{until}$  no more patterns $\underline{return} |w_j, w_2, ...$ 

end

#### Program descriptions

### Syntax:

[clusters, cluster\_labels] = Leader\_Follower(patterns, targets, input\_parameters, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = Leader\_Follower(patterns, targets, input\_parameters, plot\_on);

[clusters, cluster\_labels, original\_data\_labels, weights] = Leader\_Follower(patterns, targets, input\_parameters, plot\_on);

# Input parameters:

- 1. The minimum distance to connect across  $\theta$ .
- 2. The rate of convergence.
- The input parameter plot\_on determines if the cluster centers are plotted during training.

## Additional outputs:

- 1. The number of the cluster assigned to each input pattern.
- 2. The weight matrix representing the cluster centers.

# **Hierarchical Dimensionality Reduction**

Function name: HDR

Description: This function clusters similar features so as to reduce the dimensionality of the data.

Pseudo-code:

**begin initialize** d',  $D_i \leftarrow \{x_i\}$ , i = 1, ..., d  $\hat{d} \leftarrow d + 1$  **do**  $\hat{d} \leftarrow \hat{d} - 1$ computer **R** find most correlated distinct clusters, say  $D_i$  and  $D_j$   $D_i \leftarrow D_i \cup D_j$  (merge) delete  $D_j$  **until**  $\hat{d} = d'$  **return** d' clusters **end** 

<u>unu</u>

Syntax:

[new\_patterns, new\_targets] = HDR(patterns, targets, input\_parameter);

### Input parameter:

The desired number of dimensions d' for representing the data.

# **Independent Component Analysis**

#### Function name: ICA

**Description**: Independent component analysis is a method for blind separation of signals. This method assumes there are N independent sources, linearly mixed to generate M signals, MŠN. The goal of this method is to find the mixing matrix that will make it possible to recover the source signals. The mixing matrix does not generate orthogonal sources (as in PCA), rather the sources are found so that they are as independent as possible. The program works in two stages. First, the data is standardized, i.e., whitened and scaled to the range [-1, 1]. The data is then rotated to find the correct mixing matrix; this rotation is performed via a nonlinear activation function. Possible functions are, for example, odd powers of the input and hyperbolic tangents.

#### Syntax:

[new\_patterns, new\_targets] = ICA(patterns, targets, input\_parameters);

[new\_patterns, new\_targets, unmixing\_mat] = ICA(patterns, targets, input\_parameters);

[new\_patterns, new\_targets, unmixing\_mat, reshaping matrix, means\_vector] = ICA(patterns, targets, input\_parameters);

### Input parameters:

- 1. The output dimension.
- 2. The convergence rate.

### Additional outputs:

- 1. The mixing matrix.
- 2. The unmixing matrix and the means of the inputs.

# **Online Single-Pass Clustering**

Function name: ADDC

#### Description:

An on-line (single-pass) clustering algorithm which accepts a single sample at each step, updates the cluster centers and generates new centers as needed. The algorithm is efficient in that it generates the cluster centers with a single pass of the data.

#### Syntax:

[cluster\_centers, cluster\_targets] = ADDC(patterns, targets, input\_parameter, plot\_on);

#### Input parameter:

The number of desired clusters.

The input parameter plot on determines if the cluster centers are plotted during training.

### **Reference**:

I. D. Guedalia, M. London and M. Werman, "An on-line agglomerative clustering method for nonstationary data," *Neural Computation*, **11**:521-40 (1999).

# **Discriminant-Sensitive Learning Vector Quantization**

Function name: DSLVQ

#### Description:

This function performs learning vector quantization (i.e., represents a data set by a small number of cluster centers) using a distinction or classification criterion rather than a traditional sum-squared-error criterion.

#### Syntax:

[new\_patterns, new\_targets] = DSLVQ(patterns, targets, input\_parameter, plot\_on);

[new\_patterns, new\_targets, weights] = DSLVQ(patterns, targets, input\_parameter, plot\_on);

#### Input parameter:

The number of desired output clusters, *c*.

The input parameter plot on determines if the cluster centers are plotted during training.

#### Additional outputs:

The final weight vectors representing cluster centers.

#### Reference

M. Pregenzer, D. Flotzinger and G. Pfurtscheler, "Distinction sensitive learning vector quantization: A new noise-insensitive classification method," *Proceedings of the 4th International Conference on Artificial Neural Networks*, Cambridge UK (1995)

# **Exhaustive Feature Selection**

Function name: Exhaustive\_Feature\_Selection

### Description:

This function searches for the combination of features that yields the best classification accuracy on a data set. The search is exhaustive in subsets of features, and each subset is tested using 5-fold cross-validation on a given classifier. Note that applying this function when there are more than 10 features is impractical.

### Syntax:

[new\_patterns, new\_targets] = Exhaustive\_Feature\_Selection(patterns, targets, input\_parameters);

[new\_patterns, new\_targets, feature\_numbers] = Exhaustive\_Feature\_Selection(patterns, targets, input\_parameters);

### **Input parameters:**

- 1. The output dimension.
- 2. The classifier type.
- 3. The parameters appropriate to the chosen classifier.

### Additional outputs:

The indexes of the selected features.

# **Information-Based Feature Selection**

Function name: Information\_based\_selection

#### Description:

This function selects the best features for classification based on information-theoretic considerations; the algorithm can be applied to virtually any basic classifier. However this program is often slow because the crossentropy between *each* pair of features must be computed. Moreover, the program may be inaccurate if the number of data points is small.

#### Syntax:

[new\_patterns, new\_targets] = Information\_based\_selection(patterns, targets, input\_parameter);

[new\_patterns, new\_targets, feature\_numbers] = Information\_based\_selection(patterns, targets, input\_parameter);

### Input parameter:

The desired number of ouput dimensions.

### Additional outputs:

The indexes of the features returned.

### Reference:

D. Koller and M. Sahami, "Toward optimal feature selection," *Proceedings of the 13th International Conference on Machine Learning*, pp. 284-92 (1996)

# Kohonen Self-Organizing Feature Map

Function name: Kohonen\_SOFM

#### **Description**:

This function clusters the data by generating a self-organized feature map or "topologically correct map."

## Syntax:

[clusters, cluster\_labels] = Kohonen\_SOFM(patterns, targets, input\_parameters, plot\_on);

[clusters, cluster\_labels, original\_data\_labels] = Kohonen\_SOFM(patterns, targets, input\_parameters, plot\_on);

### Input parameter:

- 1. The number of desired output clusters, c.
- 2. Window width.

The input parameter plot\_on determines if the cluster centers are plotted during training.

### Additional outputs:

# **Multidimensional Scaling**

Function name: MDS

#### Description:

This function represents a data set in a lower dimensional space such that if two patterns  $x_1$  and  $x_2$  are close in the original space, then their images  $y_1$  and  $y_2$  in the final space are also close. Conversely, if two patterns  $x_1$  and  $x_3$  are far apart in the initial space, then their images  $y_1$  and  $y_3$  in the final space are also far apart. The algorithm seeks an optimum of a global criterion function chosen by the user.

#### Syntax:

[clusters, cluster\_labels] = MDS(patterns, targets, input\_parameters);

### **Input parameters:**

1. The criterion function  $J_{ee}$ ,  $J_{ef}$ , or  $J_{ff}$  (ee - emphasize errors, ef - emphasize large products of errors and fractional errors, or ff - emphasize large fractional errors).

- 2. The number of output dimensions.
- 3. The convergence rate.

# **Minimum Spanning Tree Clustering**

Function name: min\_spanning\_tree

#### **Description**:

This function builds a minimum spanning tree for a data set based on either nearest neighbors or inconsistent edges.

## Syntax:

[clusters, cluster\_labels] = min\_spanning\_tree(patterns, targets, input\_parameters, plot\_on);

#### Input parameter:

1. The linkage determination method (NN - nearest neighbor, inc - inconsistant edge).

2. The number of output data points per cluster or difference factor.

The input parameter plot\_on determines if the cluster centers are plotted during training.

# **Principle Component Analysis**

#### Function name: PCA

#### **Description**:

This function implements principle component analysis. First the algorithm subtracts the sample mean from each data point. Then the program computes the eigenvectors of the covariance matrix of the data and selects the largest eigenvalues and associated eigenvectors. The data is then transformed to a new hyperspace by multiplying them with these eigenvectors.

#### Syntax:

[new\_patterns, new\_targets] = PCA(patterns, targets, input\_parameter);

[new\_patterns, new\_targets, unmixing\_mat] = PCA(patterns, targets, input\_parameter);

[new\_patterns, new\_targets, unmixing\_mat, reshaping matrix, means\_vector] = PCA(patterns, targets, input\_parameter);

#### Input parameter:

The output dimension.

### Additional outputs:

- 1. The mixing matrix.
- 2. The unmixing matrix and the means of the inputs.

# **Nonlinear Principle Component Analysis**

Function name: NLPCA

### **Description**:

The function implements a neural network with three hidden layers: a central layer of linear units and two nonlinear sigmoidal hidden layers. The number of units in the central linear layer is set equal to the desired output dimension. The network is trained as an auto-associator—i.e., mapping input to the same target input—and the nonlinear principle components are represented at the central linear layer.

### Syntax:

[new\_patterns, new\_targets] = NLCA(patterns, targets, input\_parameters);

### **Input parameters:**

- 1. The number of desired output dimensions.
- 2. The number of hidden units in the nonlinear hidden layers.

# **Kernel Principle Component Analysis**

Function name: kernel\_PCA

#### **Description**:

This function implements principle component analysis with kernel functions. This algorithm is identical to principle component analysis, except that the data is first mapped to a new space using a kernel function

#### Syntax:

[new\_patterns, new\_targets] = kernel\_PCA(patterns, targets, input\_parameter);

#### Input parameters:

- 1. The output dimension.
- 2. The kernel function: Gauss (or RBF), Poly, Sigmoid, or Linear.
- 3. Kernel parameter: For each kernel parameters the following parameters are needed:
- RBF kernel: Gaussian width (scalar parameter)
- Poly kernel: The integer degree of the polynomial
- Sigmoid: The slope and constant of the sigmoid
- Linear: no parameters are needed

# **Linear Vector Quantization 1**

Function name: LVQ1

### Description:

This function finds a representative cluster centers for labeled data, and can thus be used as a clustering or as a classification method. The program moves cluster centers toward patterns that are in the same class as the centers, and moves other centers away from those patterns of other classes.

#### Syntax:

[clusters, cluster\_labels] = LVQ1(patterns, targets, input\_parameters, plot\_on);

### Input parameter:

The number of output data points.

The input parameter plot\_on determines if the cluster centers are plotted during training.

# **Linear Vector Quantization 3**

Function name: LVQ3

### **Description**:

This function finds a representative cluster centers for labeled data, and can thus be used as a clustering or as a classification method. The program moves cluster centers toward patterns that are in the same class as the centers, and moves other centers away from those patterns of other classes. LVQ3 differs from LVQ1 in details of the rate of the weight updates.

### Syntax:

[clusters, cluster\_labels] = LVQ3(patterns, targets, input\_parameters, plot\_on);

### Input parameter:

The number of output data points.

The input parameter plot\_on determines if the cluster centers are plotted during training.

# **Sequential Feature Selection**

Function name: Sequential\_Feature\_Selection

#### **Description**:

This function sequentially selects features for the lowest classification error. Then, until enough features are found, a feature that gives the largest reduction in classification error is added to the set. For backward selection, the process begins with the full set of features, and one is removed at each iteration.

#### Syntax:

[new\_patterns, new\_targets] = Sequential\_Feature\_Selection(patterns, targets, input\_parameters);

[new\_patterns, new\_targets, feature\_numbers] = Sequential\_Feature\_Selection(patterns, targets, input\_parameters);

#### **Input parameters:**

- 1. The choice of search (Forward or Backward).
- 2. The output dimension.
- 3. The classifier type.
- 4. The parameters appropriate to the chosen classifier.

#### Additional outputs:

The indexes of the selected features.

# **Genetic Culling of Features**

Function name: Genetic\_Culling

#### **Description**:

This function performs feature selection using a genetic algorithm of the culling type, i.e., it selects subsets. The algorithm randomly partitions the features into groups of size  $N_g$ . Each candidate partition is evaluated for classification accuracy using five-fold cross validation. Then, the algorithm deletes a fraction of the worst-performing groups and generate the same number of groups by sampling from the remaining groups. The whole process then iterates until a criterion classification performance has been achieved or there is negligable improvement.

#### Syntax:

[new\_patterns, new\_targets] = Sequential\_Feature\_Selection(patterns, targets, input\_parameters);

[new\_patterns, new\_targets, feature\_numbers] = Sequential\_Feature\_Selection(patterns, targets, input\_parameters);

#### **Input parameters:**

- 1. The fraction of groups discarded at each iteration.
- 2. The number of features in each solution (The output dimension).
- 3. The classifier type.
- 4. The parameters appropriate to the chosen classifier.

#### Additional outputs:

The indexes of the selected features.

## **Reference**:

E. Yom-Tov and G. F. Inbar, "Selection of relevant features for classification of movements from single movement-related potentials using a genetic algorithm," 23rd Annual International Conference of the IEEE Engineering in Medicine and Biology Society (2001).
# References

**1** R. O. Duda, P. E. Hart and D. G. Stork, **Pattern Classification** (2nd ed.), Wiley (2001)

- 2 The MathWorks, Inc., MATLAB: The Language of Technical Computing, The MathWorks, Inc. (2003)
- 3 K. Rose, "Deterministic annealing for clustering, compression, classification, regression, and related optimization problems," *Proceedings of the IEEE*, 86(1):2210-39 (1998)
- 4 K.-R. Müller, S. Mika, G. Rätsch, K. Tsuda and B. Schölkopf, "An introduction to kernel-based learning algorithms," *IEEE Transaction on Neural Networks*, 12(2): 181-201 (2001)

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